

Simplify: $\frac{(2u)^u}{u-1} + \frac{1^{(u-1)}}{u} - \frac{2u-1}{u^2-u}$.

$$\begin{aligned} u-1 &= (u-1) \\ u &= u \\ u^2-u &= (u-1)u \\ \text{LCD} &= (u-1)u \end{aligned}$$

$$\frac{2u^2}{u(u-1)} + \frac{u-1}{u(u-1)} - \frac{2u-1}{u(u-1)}$$

$$\begin{aligned} \frac{2u^2 + u-1 - 2u+1}{u(u-1)} &= \frac{2u^2 - u}{u(u-1)} = \frac{u(2u-1)}{u(u-1)} \\ &= \frac{2u-1}{u-1} \end{aligned}$$

Simplify: $\frac{(v)^{(v-1)}}{v+1} + \frac{(3)^{(v+1)}}{v-1} - \frac{6}{v^2-1}$.

$$v+1 = (v+1) \cancel{(v+1)}$$

$$v-1 = \cancel{(v-1)}(v-1)$$

$$v^2-1 = (v+1)(v-1)$$

$$\text{LCD} = (v+1)(v-1)$$

$$\frac{v^2-v}{(v+1)(v-1)} + \frac{3v+3}{(v+1)(v-1)} - \frac{6}{(v+1)(v-1)}$$

$$\begin{aligned} \frac{v^2-v+3v+3-6}{(v+1)(v-1)} &= \frac{v^2+2v-3}{(v+1)(v-1)} = \frac{(v+3)(v-1)}{(v+1)(v-1)} \\ &= \frac{v+3}{v+1} \end{aligned}$$

Simplify: $\frac{(3w)^{w+7}}{w+2} + \frac{(2)^{w+2}}{w+7} - \frac{17w+4}{w^2+9w+14}$.

$w+2 = (w+2)$
 $w+7 = (w+7)$
 $w^2+9w+14 = (w+2)(w+7)$
 $LCM = (w+2)(w+7)$

$$\frac{3w^2+21w}{(w+2)(w+7)} + \frac{2w+4}{(w+2)(w+7)} - \frac{17w+4}{(w+2)(w+7)}$$

$$\frac{3w^2+21w+2w+4-17w-4}{(w+2)(w+7)} = \frac{3w^2+6w}{(w+2)(w+7)} = \frac{3w(w+2)}{(w+2)(w+7)}$$

$$= \frac{3w}{w+7}$$